

2, page 470, solution 32.41: The final answer is OK.

However, all of the 100s should be 110.

$$H(x) = \int_0^x h(t) dt = \int_0^x 2/(110 - t) dt = -2\{\ln(110 - x) - \ln(110)\}.$$

$$S(x) = \exp[-H(x)] = \{(110 - x)/110\}^2 = (1 - x/110)^2, \text{ for } 0 \leq x < 110.$$

$$e(30) = \int_{30}^{110} S(t) dt / S(30) = \int_{30}^{110} (1 - x/110)^2 dt / (1 - 30/110)^2$$

$$= (110/3)(1 - 30/110)^3 / (1 - 30/110)^2 = (110 - 30)/3 = \mathbf{26.67}.$$

Comment: Generalized DeMoivre's Law with  $\omega = 110$  and  $\alpha = 2$ .  $\mu(x) = \alpha/(\omega - x)$ ,  $0 \leq x < \omega$ .

$$e(x) = (\omega - x)/(\alpha + 1) = (110 - x)/3.$$

The remaining lifetime at age 30 is a Beta Distribution with  $a = 1$ ,  $b = 2$ , and  $\theta = \omega - 30 = 80$ .